

# Schilthuis Aquifer expansion @model

## Motivation

The most accurate way to simulate [Aquifer Expansion](#) (or shrinkage) is [full-field 3D Dynamic Flow Model](#) where [Aquifer Expansion](#) is treated as one of the fluid phases and accounts of geological heterogeneities, gas fluid properties, [relperm](#) properties and heat exchange with surrounding rocks.

Unfortunately, in many practical cases the detailed information on the [aquifer](#) is not available which does not allow a proper modelling of [aquifer](#) expansion using a geological framework.

Besides many practical applications require only knowledge of cumulative water influx from [aquifer](#) under pressure depletion.

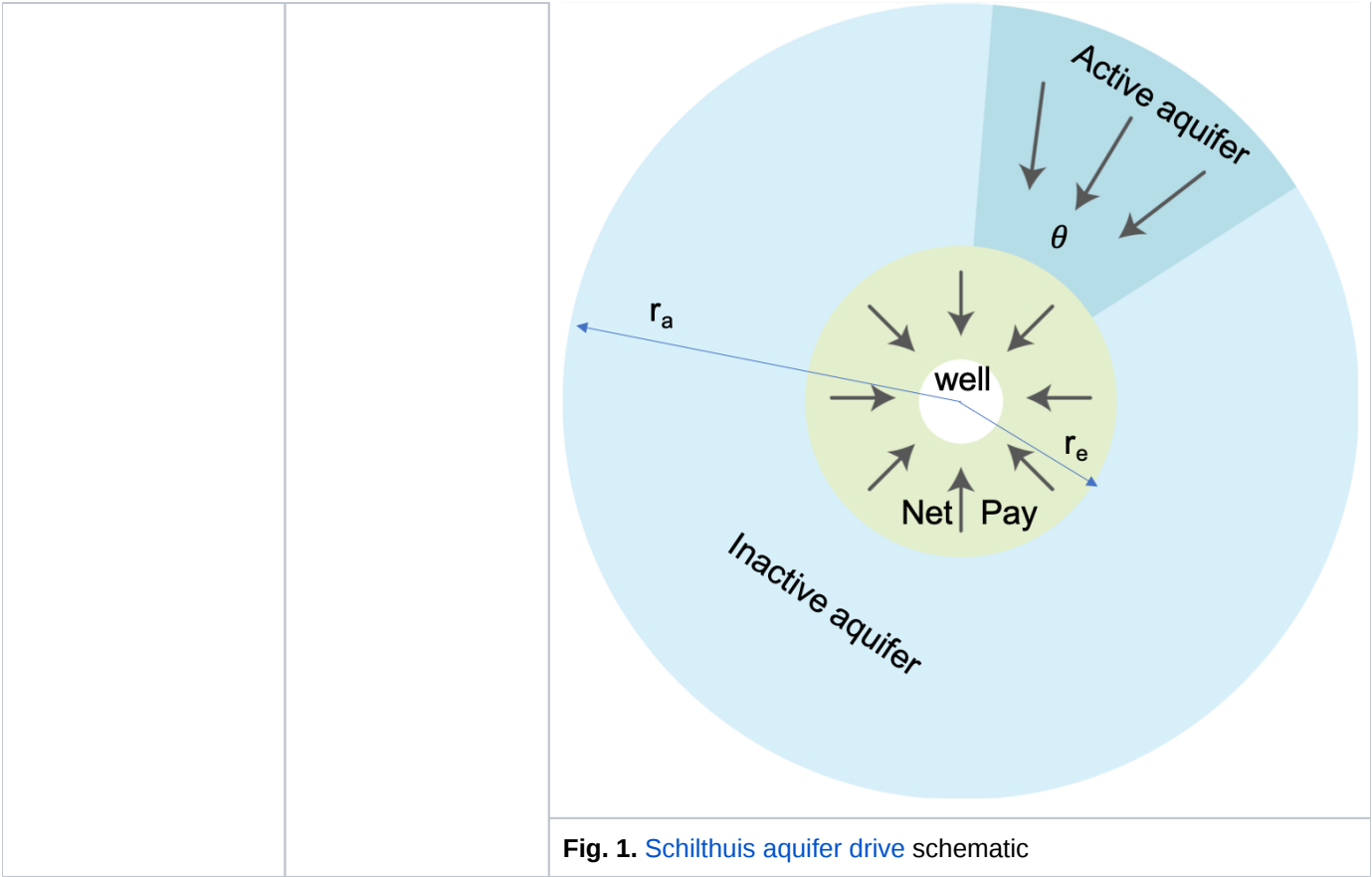
This allows building an [Aquifer Drive Models](#) using analytical methods.

## Inputs & Outputs

| Inputs   |                                                                     | Outputs                                                    |                                                                                 |
|----------|---------------------------------------------------------------------|------------------------------------------------------------|---------------------------------------------------------------------------------|
| $p(t)$   | <a href="#">field-average formation pressure</a> at time moment $t$ | $Q_{AQ}^{\downarrow}(t)$                                   | Cumulative <a href="#">subsurface water</a> influx from <a href="#">aquifer</a> |
| $p_i$    | <a href="#">initial formation pressure</a>                          | $q_{AQ}^{\downarrow}(t) = \frac{dQ_{AQ}^{\downarrow}}{dt}$ | <a href="#">Subsurface water flowrate</a> from <a href="#">aquifer</a>          |
| $J_{AQ}$ | <a href="#">aquifer Productivity Index</a>                          |                                                            |                                                                                 |

## Physical Model

|                                                        |                                  |  |
|--------------------------------------------------------|----------------------------------|--|
| <a href="#">Radial Composite Reservoir</a>             |                                  |  |
| <a href="#">Steady-state flow</a>                      |                                  |  |
| <a href="#">Aquifer</a> pressure is constant           | $p_{AQ}(t) = p_i = \text{const}$ |  |
| <a href="#">Aquifer Productivity Index</a> is constant | $J_{AQ} = \text{const}$          |  |



## Mathematical Model

|                                                                                      |                                                     |
|--------------------------------------------------------------------------------------|-----------------------------------------------------|
| $(1) \quad Q_{AQ}^l(t) = J_{AQ} \cdot \left[ p_i \cdot t - \int_0^t p(t) dt \right]$ | $(2) \quad q_{AQ}^l(t) = J_{AQ} \cdot (p_i - p(t))$ |
|--------------------------------------------------------------------------------------|-----------------------------------------------------|

It maybe considered as partial case of [Fetkovich Aquifer Drive @model](#) with infinite [Aquifer](#) volume.

## See Also

[Petroleum Industry](#) / [Upstream](#) / [Subsurface E&P Disciplines](#) / [Field Study & Modelling](#) / [Aquifer Drive](#) / [Aquifer Drive Models](#)

## Reference

- Schilthuis, R.J. 1936. Active Oil and Reservoir Energy. Trans., AIME 118: 33. <https://doi.org/10.2118/936033-G>