## Coefficient of determination = R2

## @wikipedia

A real number characterising the real-value model prediction quality (goodness of fit):

$$R^2 = 1 - \frac{MSD(x, \hat{x})}{MSD(x, \bar{x})} = 1 - \frac{\sum_i (x_i - \hat{x}_i)^2}{\sum_i (x_i - \bar{x})^2}$$

## where

$x = \{x_1, x_2, x_3, \dots x_N\}$	observed variable represented by a discrete dataset of numerical samples
$\hat{x} = {\hat{x}_1, \hat{x}_2, \hat{x}_3, \dots \hat{x}_N}$	predictor of variable $x$ , represented by another discrete dataset of numerical samples,
	with the same number of samples $N$ predicted at the same conditions as the original samples $\{x_1, x_2, x_3, \dots x_N\}$
$\bar{x} = \frac{1}{N} \sum_{i} x_{i}$	mean value of the variable $x$ , which can be considered as some sort of extreme predictor with zero variability
$MSD(x,\hat{x})$	mean square deviation between a variable $x$ and its predictor $\hat{x}$
$MSD(x,\bar{x})$	mean square deviation between a variable $x$ and its mean value $\bar{x}$

It is similar to Mean Square Deviation (MSD) but quantifies the model prediction efficiency in normalized way which is normally more suitable for assessment goodness of fit.

The coefficient of determination  $R^2$  normally ranges between:

• 0, indicating that prediction error is within the variance of the observed variable around its mean value

and

• 1, indicating a fine fit, fairly reproducing the variability of the x

The  $R^2$  values falling outside the above range indicate a substantial mismatch between variable x and model prediction  $\hat{x}$  and have a meaning that gap between predicted and actual values is higher than the variance of the actual data.

## See also

Formal science / Mathematics / Statistics / Statistical Metric