

# Travel Time (of seismic wave)

Total time required for seismic wave to travel through the rock towards the seismic receiver:

$$T_x = \int_0^{L_x} \frac{dl}{V_p(l)}$$

where

$\{x, y, z\}$  is cartesian coordinates in 3D space with  $x$ -axis aligned between seismic source and seismic sensor,  $y$ -axis is traversal to  $x$ -axis and  $z$ -axis is oriented towards Earth centre,

$x$  is a lateral offset between the seismic source and seismic receiver

$l(x, y, z)$  – trajectory of reflection wave from seismic source @  $(x = 0, y = 0, z = 0)$  and seismic receiver @  $(x, y = 0, z = 0)$

$dl = \sqrt{dx^2 + dy^2 + dz^2}$  is differential element of the distance along the reflection travel trajectory,

$V_p(l)$  is p-wave velocity of rocks found at travel point  $l$ .

blocked URL

In relatively simple geological structures the travel time can be approximated by a Dix equation:

$$(1) \quad T_x^2 = T_0^2 + \frac{4x^2}{V_{rms}^2}$$

where  $T_0^2$  is reflection time at zero offset (which means the normal incident wave reflection):

$$T_0 = 2 \cdot \int_0^H \frac{\delta z}{V_p(z)}$$

where  $H$  is the depth of the reflecting boundary,

$V_{rms}$  – average p-wave velocity through the reflecting travel distance between the seismic source and seismic receiver:

$$V_{rms}^2 = \frac{\sum_i^N V_p^2(t_i) \delta t_i}{\sum_i^N \delta t_i} = \frac{\sum_i^N V_p(t_i) \delta h_i}{\sum_i^N \frac{\delta h_i}{V_p(t_i)}}$$

where

$V_p(t_i)$  is p-wave velocity of rocks found at travel time  $t_i$ ,

$\delta t_i$  is travel time through the rock element of thickness  $\delta h_i$  in the rock element found at travel time  $t_i$ .